



# YEAR 3

## MAIN PRINCIPLES

Scan QR codes to be directed to the MNP website with further information and videos.

### What is maths mastery?

Teaching maths for mastery is a transformational approach to maths teaching which stems from high performing Asian nations such as Singapore. When taught to master maths, children develop their mathematical fluency without resorting to rote learning and are able to solve non-routine maths problems without having to memorise procedures.



### Concrete, pictorial, abstract (CPA)

Concrete, pictorial, abstract (CPA) is a highly effective approach to teaching that develops a deep and sustainable understanding of maths. Developed by American psychologist, Jerome Bruner, the CPA approach is essential to maths teaching in Singapore.



### Number bonds

Number bonds are a way of showing how numbers can be combined or split up. They are used to reflect the 'part-part-whole' relationship of numbers.



### Bar modelling

The bar model method is a strategy used by children to visualise mathematical concepts and solve problems. The method is a way to represent a situation in a word problem, usually using rectangles.



### Fractions

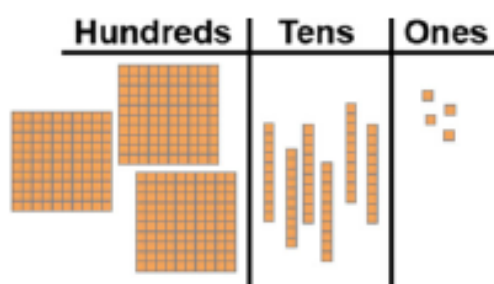
In Singapore, the understanding of fractions is rooted in the Concrete, Pictorial, Abstract (CPA) model, where children use paper squares and strips to learn the link between the concrete and the abstract. At the heart of understanding fractions is the ability to understand that we're giving an equal part a name.



# YEAR 3

## PLACE VALUE

Base ten or dienes blocks:



Value of digits:

hundreds	tens	ones
4	2	7

$427 = 4 \text{ hundreds} + 2 \text{ tens} + 7 \text{ ones}$

$427 = 400 + 20 + 7$

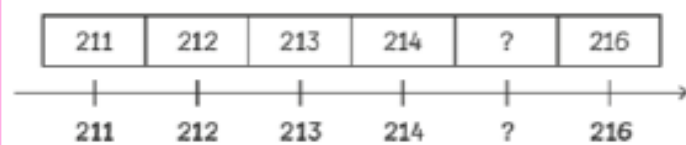
The digit 4 stands for 4 hundreds or 400.

The digit 2 stands for 2 tens or 20.

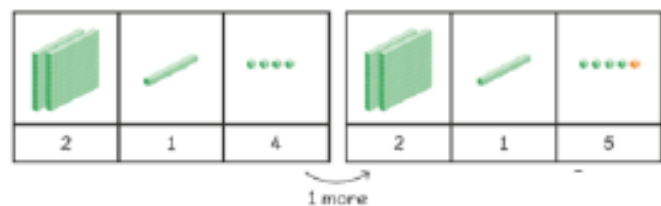
The digit 7 stands for 7 ones or 7.

We write 427 as four hundred and twenty-seven.

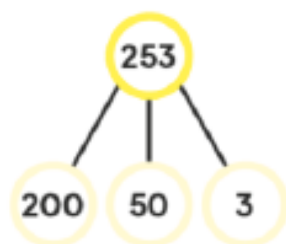
Number lines:



Finding 1 more or less than:



Number bond method:

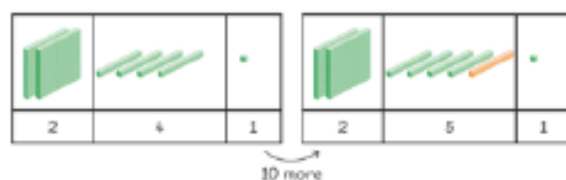


Place value cards:

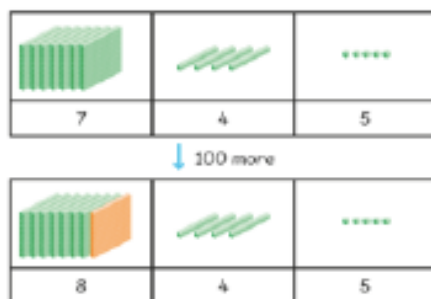


Separating the numbers apart like this is called **partitioning**.

Finding 10 more or less than:



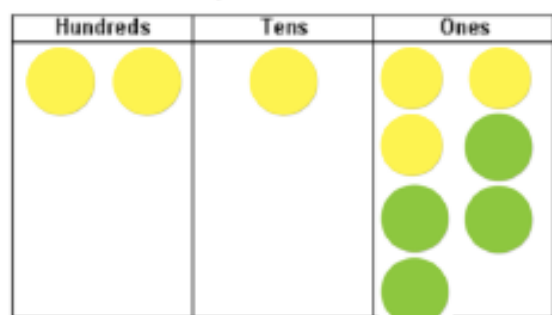
Finding 100 more or less:



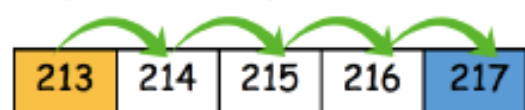
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## ADDITION

Counters method:



Number line method:



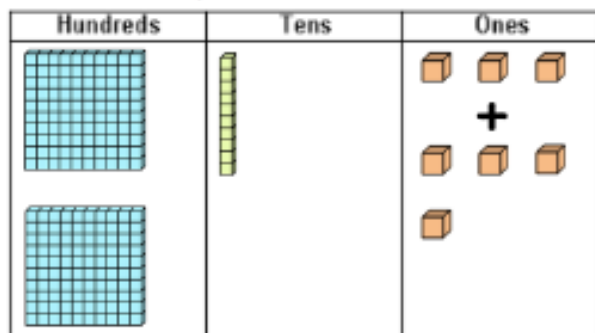
Number bond method:



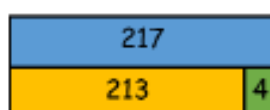
Abstract calculations:

Commutative	Inverse
$213 + 4 = 217$	$217 - 4 = 213$
$4 + 213 = 217$	$217 - 213 = 4$

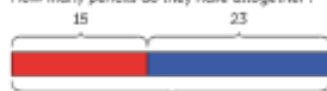
Base 10 method:



Bar model:



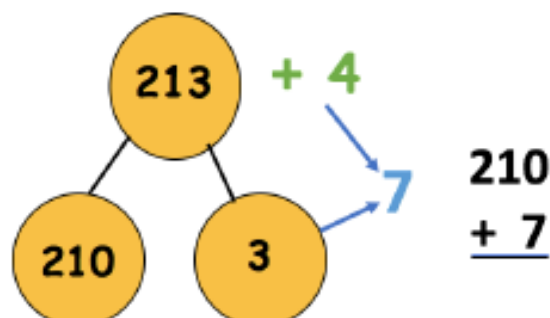
How many pencils do they have altogether?



$$15 + 23 = 38$$

They have 38 pencils altogether.

Number bond method:



Column addition:

Without renaming:

$$\begin{array}{r} 213 \\ + \quad 4 \\ \hline 217 \end{array}$$

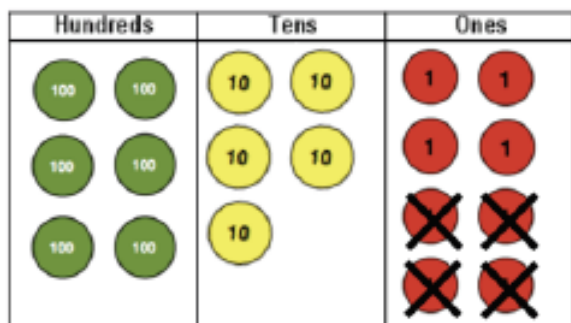
With renaming:

$$\begin{array}{r} 1 \quad 1 \\ 213 \\ + 497 \\ \hline 710 \end{array}$$

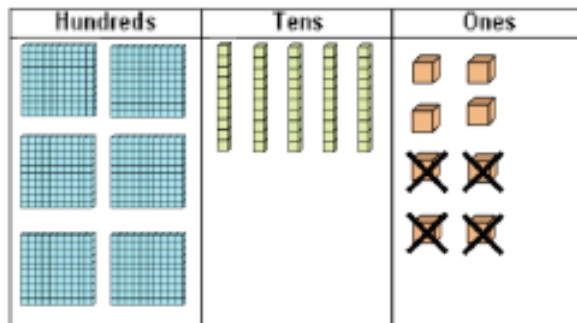
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## SUBTRACTION

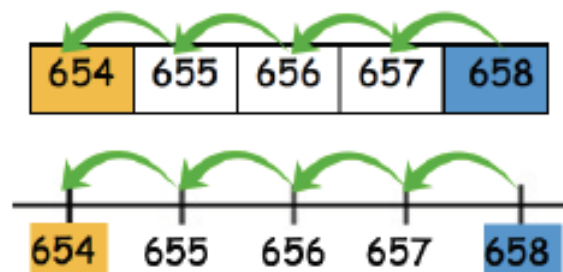
### Counters method:



### Base 10 method:



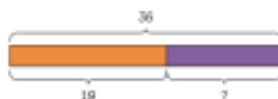
### Number line method:



### Bar models:

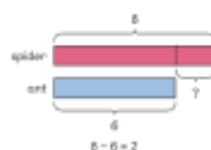
#### Bar model:

There are 36 children in the school band.  
19 of them are boys.  
How many girls are there?



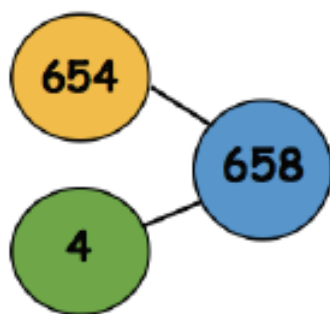
#### Comparative model:

A spider has 8 legs.  
An ant has 6 legs.

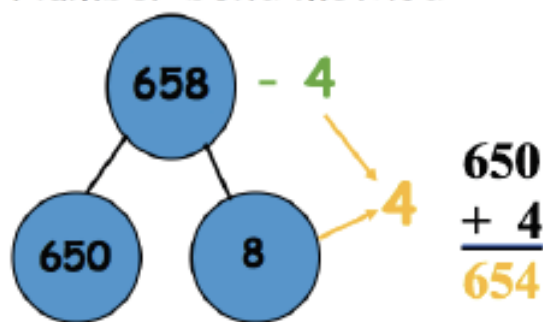


A spider has 2 more legs than an ant.

### Number bond method:



### Number bond method:



### Abstract calculations:

Commutative	Inverse
$658 - 4 = 654$	$654 + 4 = 658$
$658 - 654 = 4$	$4 + 654 = 658$

### Column subtraction:

#### Without renaming:

$$\begin{array}{r} 658 \\ - \quad 4 \\ \hline 654 \end{array}$$




#### With renaming:

$$\begin{array}{r} 6\overset{4}{\cancel{5}}\overset{1}{8} \\ - 349 \\ \hline 309 \end{array}$$

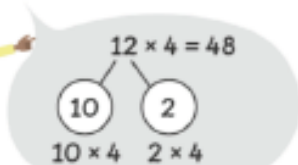
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## MULTIPLICATION

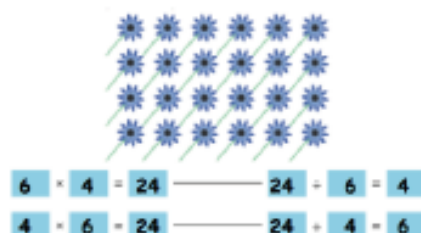
### Arrays:

3 times tables	4 times tables	8 times tables
		
$3 \times 5 = 15$	$4 \times 5 = 20$	$8 \times 5 = 40$ <small>(doubling the 4 times tables)</small>

### Number bond strategy: Multiplication

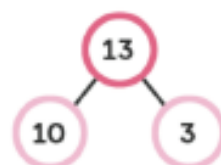


### Make a family of multiplication and division facts:



### Bridged column method: Without renaming

$$13 \times 3 = 39$$



	t	o
$\times$	1	3
		3
		9
$+$	3	0
	3	9

### Bridged column method: With renaming

Multiply the ones by 4.

	t	o
$\times$	2	5
		4
	2	0

5 ones  $\times 4 = 20$  ones  
20 ones = 2 tens

Multiply the tens by 4.

	t	o
$\times$	2	5
		4
	2	0
	8	0

2 tens  $\times 4 = 8$  tens

Add the products.

	h	t	o
$\times$		2	5
			4
		2	0
$+$		8	0
	1	0	0

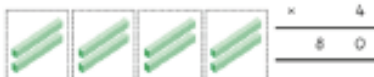
$20 + 80 = 100$

### Short multiplication: Without renaming

$$2 \times 4 = 8$$



$$2 \times 40 = 80$$



### Short multiplication: With renaming

Multiply the ones by 4.

	2 tens	t	o
$\times$		2	7
		4	4
		8	

8 ones

7 ones  $\times 4 = 28$  ones  
28 ones = 2 tens + 8 ones

Multiply the tens by 4.

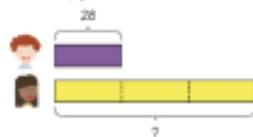
	h	t	o
$\times$		2	7
		4	4
	1	8	8

4 tens  $\times 4 = 16$  tens  
16 tens + 2 tens = 18 tens

### Solving word problems: Bar model

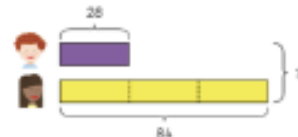
There are 28 boys in a group.  
There are 3 times as many girls as there are boys.

(a) How many girls are there?



$28 \times 3 = 84$   
There are 84 girls.

(b) How many children are there?



$28 + 84 = 112$   
There are 112 children altogether.

# YEAR 3

## DIVISION

### Grouping: 'groups of'

Put 8 🍪 into groups of 4.



$8 \div 4 = 2$   
2 plates are needed.

"I have made groups of 4.  
There are 2 equal groups.  
There are 4 in each group.  
2 equal groups of 4 equals 8."

### Grouping: 'equal groups'

Put 8 🍪 into 4 equal groups.



$8 \div 2 = 4$   
4 trays are needed.

"There are 4 equal groups.  
There are 2 in each group.  
4 equal groups of 2 equals 8."

### Number bond strategy: Division

6 tens  $\div$  2  
= 3 tens

$$68 \div 2 = 34$$

8 ones  $\div$  2  
= 4 ones



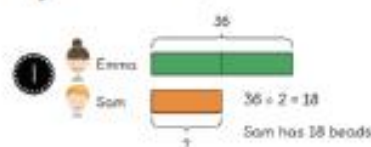
6 tens  $\div$  2

8 ones  $\div$  2



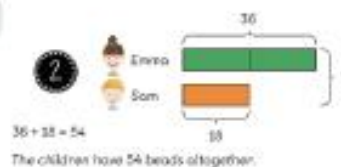
### Solving word problems: Bar model

How many beads do the children have altogether?



I have 36 beads.

She has twice as many beads as I have.



### Make a family of multiplication and division facts:



$$6 \times 4 = 24 \quad 24 \div 6 = 4$$

$$4 \times 6 = 24 \quad 24 \div 4 = 6$$

### Number bond and long division:



First, I take 80 from 96.  
Then, I take 16 from the remaining 16.



16 ones  $\div$  8 = 2 ones

$$\begin{array}{r} 12 \\ 8 \overline{) 96} \\ \underline{- 80} \phantom{0} \\ 16 \\ \underline{- 16} \\ 0 \end{array}$$

2 ones



8 tens  $\div$  8 = 1 ten

$$\begin{array}{r} 12 \\ 8 \overline{) 96} \\ \underline{- 80} \phantom{0} \\ 16 \\ \underline{- 16} \\ 0 \end{array}$$

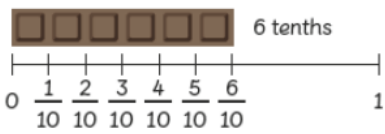


1 ten + 2 ones = 12  
 $96 \div 8 = 12$

$$\begin{array}{r} 12 \\ 8 \overline{) 96} \\ \underline{- 80} \phantom{0} \\ 16 \\ \underline{- 16} \\ 0 \end{array}$$

# YEAR 3 FRACTIONS

## Counting in tenths



## Subtracting fractions with same denominator

Subtract  $\frac{1}{9}$  from  $\frac{5}{9}$ .



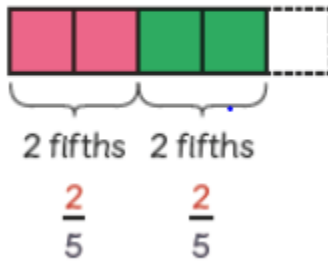
$$\frac{5}{9} - \frac{1}{9} = \square$$

5 ninths - 1 ninth =    ninths



## Add fractions with same denominator

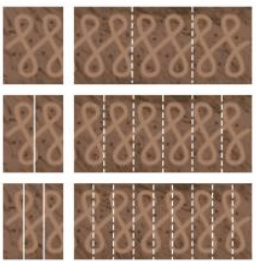
Add  $\frac{2}{5}$  and  $\frac{2}{5}$ .



$$\frac{1}{4} + \frac{3}{4} = \frac{4}{4} = 1$$

## Equivalent Fractions

What can you say about  $\frac{1}{4}$ ,  $\frac{2}{8}$  and  $\frac{3}{12}$ ?



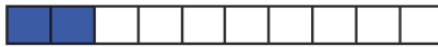
1 fourth

2 eighths

3 twelfths

Concrete

pictorial



This is  $\frac{2}{10}$ .

$$\frac{1}{5} = \frac{2}{10}$$

× 2 (above the line)  
× 2 (below the line)



Abstract

## Finding part of a set



$\frac{1}{6}$  of 12 doughnuts = 2 doughnuts

$\frac{5}{6}$  of 12 doughnuts =  $5 \times 2$  doughnuts = 10 doughnuts



## Sharing more than one

2

2 pies shared by 3 children  
 $2 \div 3$

Cut each pie into 3 equal parts.

$$2 \div 3 = \frac{2}{3}$$

Each child gets 2 thirds of a pie.

